# LNO<sub>x</sub> in deep convection as simulated by an explicit charging and discharge lightning scheme implemented within the WRF-ARW model

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**ABSTRACT:** In order to study the characteristics of  $LNO_X$  in deep convection, this study presents numerical simulations of the generation and transport of LNO<sub>X</sub> via a new explicit lightning model implemented within WRF-ARW featuring explicit inductive and non-inductive charging processes. The test case is the 10 July 1996 STERAO storm. The isolated storm evolved from a multicellular thunderstorm to a quasi-supercell. Three convective cells were initiated in the domain, oriented northwest-southeast. After one hour, the updraft of middle cell was weak, with correspondingly low liquid water content and low ice crystal and graupel mixing ratios, resulting in less lightning and NO<sub>X</sub>. The other two stronger cells had more lightning and LNO<sub>X</sub> production. In general, LNO<sub>X</sub> was distributed in the net charge regions, but did not follow an obvious relationship with charge density. The peak  $LNO_X$ concentration (2.0-5.0 ppbv) was near the top of the updraft within a region of relatively high ice crystal and graupel concentration. Another peak in  $LNO_X$  (1.0-2.5ppbv) was located in a region extending from the ground up to an altitude of 3 km, under the lower positive charge center. The stronger the cell is, the more obvious the lower peak LNO<sub>X</sub> becomes. LNO<sub>X</sub> was lower (0.25-0.5ppbv) between 3-7km height, corresponding to the strong updraft region and reduced production. The LNO<sub>X</sub> distribution within this simulated storm exhibits a noticeable "C" shape. After 2-4 h of simulation, the storm gradually evolved from a multicellular thunderstorm to a quasi-supercell. The maximum  $LNO_X$  content exceeded 5ppbv for a period within a broader area.

#### INTRODUCTION

Lightning-produced NO<sub>X</sub> (LNO<sub>X</sub>) is a major source of tropospheric nitrogen oxides (NO<sub>X</sub>=NO+ NO<sub>2</sub>). Research for LNO<sub>X</sub> is helpful to understand the feedback of lightning activity to climate  $\circ$ 

Zel'dovich and Raizer [1967] first provided the chemical equations of  $LNO_X$ . Nitric oxide (NO) is produced in very hot (about 30,000K) lightning channels due to oxygen (O<sub>2</sub>) and nitrogen (N<sub>2</sub>) dissociation. As the channels cool to 3000-4000 K, NO is formed in the resulting plasma and is "frozen in" during the subsequent cooling to ambient temperature. Within seconds NO is converted to NO<sub>2</sub> by

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reaction with ambient ozone  $(O_3)$ . NO<sub>2</sub> can be photolysed back to NO during daytime. An equilibrium is reached after about 100 s, known as the photostationary state. Wang et al. [1998] studied the production of NO by means of arc discharges in the laboratory. Their results were accepted to be the most accurate results among similar experiments. They found that production of NO<sub>2</sub> was less than 10% of the production of NO in arc discharge. So, most research has studied the characteristics of LNO<sub>X</sub> through estimating the production of lightning-produced NO.

Many previous studies implement LNO<sub>x</sub> scheme in high resolution cloud-resolving models. The first type of parameterization distributes LNO<sub>x</sub> based on observed or simply-paramerized lightning flash rate. [Pickering et al. 1998, Wang and Prinn 2000, DeCaria et al., 2000,2005]. The second type of LNO<sub>x</sub> parameterization in cloud model is based on explicit microphysical charge separation and discharge mechanisms. Zhang et al. [2003] first added a LNO<sub>x</sub> parameterization into 3-D Storm Electrification Model (SEM) with an explicit and completed charging mechanism parameterization. An unbranched lightning channel propagated along the electrical field vector and presented quasi-vertically according to Kasemir [1960, 1983]. The lightning discharge parameterization only simulated IC flashes, and without branching could not include horizontal channels, which can extend to tens of kilometers. LNO<sub>x</sub> distributed in a given volume around lightning channel in proportion to lightning released energy and neutralized charge according to a certain ratio. NO production was set to be  $9.2 \times 10^{16}$  molecules/J. For their simulation, a number of chemical reactions among NO, NO<sub>2</sub> and O<sub>3</sub> were considered. Simulated lightning frequency was much less than that observed.

Barthe et al.[2007] implemented an explicit  $LNO_X$  scheme in the 3-D mesoscale model Meso-NH [Barthe et al.,2005] with a complete electrification and lightning flash scheme [Barthe et al. 2005]. The electric charges were carried by each of the five hydrometeor categories of the mixed phase microphysical scheme. They were mostly separated by elastic ice-graupel collisions, known as a non-inductive process. The lightning flash scheme, based on MacGorman et al. [2001] consisted of two parts: a quasi-vertical bidirectional leader and growing branching streamers. The leader was triggered and propagates according to the ambient electrical field. Branches were generated by an iterative algorithm. The maximum number of branches at a given distance from the initiation point obeyed a fractal law. The scheme mimics branches and especially the horizontal extension of IC flashes. This model adapted the method of Wang et al [1998], where the LNO<sub>X</sub> production was proportional to the lightning flash length and depended on the atmospheric pressure. No chemistry was considered in their model.

Barth et al. [2007] simulated the storm case of 10 July 1996 STERAO (Stratopheric-Tropospheric Experiment: Radiation, Aerosols, and Ozone) by using eight different cloud models and described the intercomparison to examine transport of six species of chemical substances. All but one of these models considered the reactions of chemical substances, and six of them included some type of lightning-produced NO<sub>X</sub>. The WRF-AqChem and UMd/GCE followed DeCaria et al. [2005]. C. Wang's convective cloud model with chemistry followed the disk model of Wang and Prinn [2000]. M. Leriche and S. Cautenet used the scheme of Pickering et al.[1998] in RAMS with an assumed NO production rate of 1113 and 111 moles NO per each CG and IC flash, respectively. J.-P.Pinty, C.Barthe and C.Mari added NO in Meso-NH along the lightning flash path as a function of the pressure and the channel length as suggested by Wang et al [1998]. The average production of NO was 36moles per flash for both CG and IC flashes.

In 3-D SEM (Storm Electrification Model) [Helsdon and Farley, 1987, and Helsdon et al., 2001] energy dissipation can be determined by calculating the electrical energy just before and immediately after the discharge. Lightning-produced NO production  $(9 \times 10^{16} \text{NO molecules J}^{-1}$  at sea level) is proportional to this electrical energy and pressure, and is limited to the immediate vicinity of the lightning channel. For this simulation, the NO production ranged from 5 to 351 moles NO per flash with a mean of 97 moles.

The results of Barth et al. [2007] indicated that models that included lightning production of  $NO_X$  reasonably predict  $NO_X$  mixing ratios in the anvil compared with observations.

In order to study the characteristic of  $LNO_X$  in deep convection, this paper presents numerical simulations of the generation and transport of  $LNO_X$  via a new explicit lightning model implemented within WRF-ARW featuring explicit inductive and non-inductive charging processes [Fierro et al. 2013]. The discrete lightning discharge scheme of MacGorman [2001] was also incorporated into the model. The lightning-generated  $NO_X$  followed the scheme of Wang et al. [1998] with assumptions of channel length within each grid cell. The test case of the 10 July 1996 STERAO storm was simulated.

#### **DESCRIPTION OF THE MODEL**

### Lightning parameterization

Fierro et al. [2013] implemented an explicit lightning physics within the Weather Research and Forecast (WRF) model. Charging of hydrometeors consists of five distinct non-inductive parameterizations, polarization of cloud water and the exchange of charge during collisional mass transfer (Mansell et al. 2010, Saunders and Peck 1998, Brooks et al. 1997). No screening layer parameterization was used for these simulations. The discharge process employs concepts adapted from two well-documented bulk lightning models [MacGorman,1994, MacGorman et al.,2001], whereby charge reduction is imposed within a prescribed volume centered at grid points characterized by electric field magnitudes exceeding a given breakdown threshold.

In order to simulate  $LNO_x$ , we employ lightning parameterization adapted from MacGorman [2001] in Ferro et al. [2013] model. Since the scheme produces few CG flashes, IC flashes were hybridized to allow a net discharge. Normally IC flashes would be limited to have equal and opposite charge deposition at the positive and negative ends. If the immediate region of the flash carried a net charge, however, the IC flash was allowed to act against that net charge if possible. For example, if the storm region had net positive charge, and the flash had more positive than negative charge available for discharge, then the flash could deposit excess negative charge into the positive region. Otherwise, IC flashes were restricted to be overall neutral.

The lightning parameterization adapted from MacGorman [2001] just can mimic the gross structure of flashes, not the detailed development of lightning channels. In this scheme, instead of stopping at larger ambient electric field magnitudes, extensive flash development can continue in regions having a weak ambient electric field but a substantial charge density and consistent electric potential, so the extension of lightning channel simulated by the new parameterization is same as lightning structure observations. Although the choice of parameter values affects the simulated lightning structure, the qualitative features of simulated flash structure are similar to those of observed lightning as long as the parameter values are consistent with the larger electric field magnitudes measured in storms and with simulated charge

densities produced over reasonably large regions. The new parameterization is computationally efficient, but less so than the bulk lightning model [Fierro et al.] because each flash is computed sequentially with a recalculation of the electric potential after each flash.

#### LNO<sub>x</sub> parameterization

We employ the LNO<sub>X</sub> parameterization adapted from Wang et al. [1998]. NO<sub>X</sub> is produced as a function of lightning channel length and pressure with a scaling based on the amount of charge deposited in a given grid cell. The molecule number  $n_{NO}^{"}$  (unit: 10<sup>21</sup> molecules/m) produced by per meter of lightning channel is,

$$n_{NO}^{"}(i,j,k) = a + bP(i,j,k)$$
(1)

Where P is pressure (unit: Pa), a=0.34, b=1.30, and i, j, k represent coordinates of discharge grid in x,y and z, respectively. The lightning-NO (unit: mol) of each grid volume is,

$$n_{NO}'(i,j,k) = l_{chan} \times n_{NO}''(i,j,k) / N_A$$
<sup>(2)</sup>

where  $l_{chan}$  is channel length (m) and is taken as the horizontal grid spacing dx,  $N_A$  is Avogadro constant, equal to  $6.022 \times 10^{23}$  mol<sup>-1</sup>.

The volume concentration of lightning-generated NO of each grid volume is,

$$n_{NO}(i,j,k) = \delta \rho'(i,j,k) \times n_{NO}'(i,j,k) \times M_{air} / (\rho_{air} \times \Delta V)$$
(3)

where  $M_{air} = 28.96 \times 10^{-3} kg \ mol^{-1}$ , is mole mass of air.  $\Delta V$  is grid volume (m<sup>3</sup>), equal to

 $dx \times dy \times dz$ , dx, dy and dz (unit: m) are grid distance in x, y and z direction, respectively.  $\rho_{air}$  is air density (kg m<sup>-3</sup>).

$$\delta \rho'(i,j,k) = \left( \left| \Delta \rho_{\pm}(i,j,k) \right| \right) / \delta q_0 \tag{4}$$

It is a ratio of neutralized charge at each discharge grid to  $\delta q_0$ .  $\Delta \rho_+(i, j, k)$  is the deposited charge density at a grid point at the positive end of the lightning, and  $\Delta \rho_-(i, j, k)$  is the deposited charge density at a grid point at the negative end.  $\delta q_0$  is a referenced charge density to scale the NO production. In this paper,  $\delta q_0 = 0.5nCm^{-3}$ . The introduction of  $\delta q_0$  is based on the laboratory result of Wang et al. [1998]. Their study showed that NO production is  $15 \times 10^{16}$  mol J<sup>-1</sup> when current in lightning channel is 10kA, while, NO production is  $40 \times 10^{16}$  mol J<sup>-1</sup> when current in lightning channel is 30kA. So, it can be inferred that a linear relationship may exist between NO production and lightning energy (current). In this paper, the neutralized charge is used to represent lightning energy, and together with a standard referenced charge density  $\delta q_0$  to correct NO production at each grid. This method is reasonable and can avoid the virtual high of simulation NO production.

## SIMULATION OF THUNDERSTORM CASE IN STERAO

The storm case of 10 July 1996 STERAO (Stratospheric-Tropospheric Experiment: Radiation, Aerosols, and Ozone) is simulated by using the WRF-ARW including explicit charging and discharge parameterization within the NSSL 2-moment microphysics scheme (Mansell et al. 2010). A major purpose of STERAO was to study the effect of lightning on chemical constituents in middle and upper troposphere, especially LNO<sub>X</sub> and NO<sub>X</sub> transport from boundary layer. Observations of the storm were obtained from several platforms including the CSU CHILL radar, the ONERA lightning interferometers, the NOAA WP3D aircraft and UND Citation aircraft [Dye et al., 2000]. This thunderstorm was observed near the Wyoming-Nebraska-Colorado border. The isolated storm evolved from a multicelluar thunderstorm to a quasi-supercell.

Previous model simulations have proven to successfully represent the observed storm [Skamarock et al. 2000, 2003, Barth et al. 2001, 2007]. The environmental was assumed to be homogeneous, thus a single profile observed by aircraft and radiosonde was used for initialization [Skamarock et al., 2000]. The convection is initiated with 3 warm bubbles (3  $^{\circ}$ C perturbation) oriented in a NW to SE line following Skamarock et al.[2000].

## **Hydrometeors**

Figure 1 shows vertical cross sections of hydrometeor mixing ratios at 1 hour and 3.5 hours. During the multicellular stage (Figure 1a), three aligned convective cells are in NW-SE direction. Each cell top reaches about 13 km altitude and has a horizontal extent of 20 km. The central cell contains a low cloud droplet mixing ratio compared to that of the two other cells, so its convection is weak.



Figure 1. Partial vertical along-wind cross section at (a) 1 hour and (b) 3.5 hours of hydrometeor mixing ratios. Colored areas, blue dashed lines, red solid lines and black solid lines represent graupel, pristine ice and snow, cloud droplet and rain drop mixing ratios respectively. The mixing ratio contours are 0.1, 0.5, 1 and 2 g kg<sup>-1</sup> for pristine ice and snow, cloud droplets and rain drops. Grey solid lines represent  $0^{\circ}$ C,  $-10^{\circ}$ C,  $-20^{\circ}$ C and  $-40^{\circ}$ C from upper to lower.

All of them have the anvil comprised of ice crystal and snow. The anvils of the northwestern and central cells overlap the cloud top of the adjacent downwind cell, and anvil of southeast cell stretches downwind to 30 km. For the middle cell, the cloud droplet mixing ratio was relatively low, and without obvious rain. At the same time, mixing ratios of graupel and hail are relatively low, less than 5 g kg<sup>-1</sup> in center, due to the lower amounts of cloud water. So, charging process is weak, and less LNO is generated. While the two other cells with little rain  $(0.1 \text{ g kg}^{-1})$  and higher cloud water, and supercooled water up to the -40°C layer. So, graupel and hail between -30°C and -40°C grow by riming, and their mixing ratios exceed 5 g kg<sup>-1</sup>. The anvil of the sourtheast cell has greater ice crystals and snow contents than two other cells and stretches farther downwind. The storm develops supercell characteristic at about 2.5 h of simulation (not shown), and the anvil stretches downwind for about 70 km. In the core convection area, mixing ratios of ice crystal and snow reach about 2 g kg<sup>-1</sup> near 10 km, cloud droplet top reaches near -40°C layer with mixing ratio exceeding 0.5 g kg<sup>-1</sup>, and graupel and hail between 4 and 10 km have mixing ratio reaching 1-5 g kg<sup>-1</sup>. Rain distributes in the area near the surface, and its mixing ratio reach to 0.1 g kg<sup>-1</sup>. During the supercellular stage (Figure 1b), the anvil extend on 100 km in the NW-SE direction. At 10.0 km altitude, the pristine ice and snow mixing ratio reaches 2 g kg<sup>-1</sup>. The maximum graupel mixing ratio remains around 5 g kg<sup>-1</sup> at 6-10 km. The cloud droplet and the rain drop mixing ratios reach 2 g kg<sup>-1</sup> and 1.5 g kg<sup>-1</sup> respectively. All the results are consistent with the simulation made by Barthe et al. [2007] using Meso-NH.

## Charge structure and reflectivity

Figure 2 shows a vertical cross section of total charge density and of reflectivity through the three multicell cores, after 1 hour and 3.5 hours of simulation. During the multicellular stage (Figure 2a), each cell is characterized by complex structure dominated by a normal dipole but with a weaker upper negative charge layer. This structure is similar as the highly stratified structure discussed by Stolzenburg et al. [1998] and different from the inverted dipole structures simulated by Barthe et al. [2007]. Barthe et al. [2007] adopted the non-inductive charging results of Takahashi [1978] and neglected the inductive mechanism. All of these in addition to different models and microphysics can cause distinctly different results. The electrification in the southeastern cell is strongest. The magnitudes of its positive and negative charge density reach 1.0 nC m<sup>-3</sup>. During the multicellular stage (Figure 2b), the charge structure is an inverted dipolar. During the two stages, the main positive and negative charge regions of cells are all located in the upper of the strongest reflectivity region, and the charge regions are limited in the area that reflectivity is more than 40 dBZ.



Figure 2 . Partial vertical along-wind cross section at (a) 1 hour and (b) 3.5 hours of net charge density (colored areas, unit: nC m<sup>-3</sup>) and radar reflectivity (contours: 20 dBZ, 40 dBZ and 60 dBZ). Grey solid lines represent 0°C, -10°C, -20°C and -40°C from upper to lower.

## LNO<sub>x</sub> production

During the multicellular stage, in the strongest convection regions (Figure 3a), LNO<sub>X</sub> distribution is limited in the whole charge region compared with Figure 2a. In the stronger convection regions (Figure 3b), LNO<sub>X</sub> mainly distributes in the upper of cloud. The peak values of NO<sub>X</sub> of both cross sections reached 2.0-5.0ppbv. The environmental of NO<sub>X</sub> is about 0.4-0.6ppbv from ground to 2 km height [Barthe et al., 2007]. The LNO<sub>X</sub> distribution within this simulated storm results from production by lightning and subsequent transport by both updrafts and downdrafts. Although environmental NOx is not included, an enhancement by lightning would certainly be evident in the anvil exhaust region as well as in downdrafts reaching the surface. [Huntrieser et al. 2002],.



Figure 3. Along-wind vertical cross section of the NO<sub>x</sub> in the multicellular stage (colored areas in pptv). The cloud limit is outlined (thick solid line). (a. the strongest convection region; b. the stronger updraft region)



Figure 4. Horizontal cross sections at (top) 12,500 m (a), (middle) 10,000 m (b) and (bottom) 7500 m (c) of the hourly LNO<sub>x</sub> concertration in logarithmic scale at 1,2,3,4 and 5 hours. Solid black lines are areas with reflectivity larger than 20 dBZ. Every horizontal domain is 100 km×100 km.

The hourly LNO<sub>X</sub> field is displayed through a series of plots in Figure 4 for three elevations: 12.500 m, 10,000 m and 7,500 m. After one hour of simulation, NO<sub>X</sub> is produced in each cell and their peak values are almost limited the convection centers. The NO<sub>X</sub> at 10 km height is the largest (1~2ppbv). Just a little LNO<sub>X</sub> is transported to downwind. After 2-4 h of simulation, the storm gradually evolved from a multicellular thunderstorm to a quasi-supercell. More and more LNO<sub>X</sub> is produced with the storm, and the peak value of LNO<sub>X</sub> exceed 5 ppbv for a short period. Due to the atmospheric turbulence and advection, the LNO<sub>X</sub> is gradually transported and diluted. So, the region of LNO<sub>X</sub> extends to downwind in the anvil in a large area, and the peak of LNO<sub>X</sub> is not more than 5 ppbv at the later time.

## CONCLUSIONS

This study presents a numerical simulation of the generation and transport of  $LNO_X$  via a new explicit lightning model implemented within WRF-ARW featuring explicit inductive and non-inductive charging processes. Via simulation of the 10 July 1996 STERAO storm, it is indicated that  $LNO_X$  is mainly produced in the charge region and then diluted and transported to downwind in the anvil in a large area.

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