## NSSL's Dual-polarization Censoring Algorithm

This technique is recommended for the first release of the dual-polarimetric WSR-88D. In general, it applies to any radar that transmits and receives simultaneously horizontally and vertically (SHV) polarized waves at a uniform PRT of duration $T_{s}$.

Let $H_{i}$ denote a complex signal (in-phase and quadrature phase) of horizontally polarized echoes at a fixed range location (same range gate) where the first echo received is $H_{0}$. The spacing between $H_{i}$ samples is $T_{s}$ and the total number of $H$ samples is $M$ (that is the index $i$ goes from 0 to $M-1$ ). Let $V_{i}$ denote a complex signal of vertically polarized echoes, the spacing between $V_{i} \mathrm{~s}$ is also $T_{s}$ and the total number of $V_{i}$ samples is also $M$. So the sequence of sample pairs is ( $H_{0}$, $\left.V_{0}\right),\left(H_{1}, V_{1}\right),\left(H_{2}, V_{2}\right),\left(H_{3}, V_{3}\right) \ldots$ etc.
The two quantities used for the censoring are the signal-to-noise (SNR) estimate in the H channel $\left(S N R_{h}\right)$ and the "uniform sum" (US). The $S N R_{h}$ is computed as
$S N R_{h}=\frac{\frac{1}{M} \sum_{i=0}^{M-1}\left|H_{i}\right|^{2}}{N_{h}}-1$,
where $N_{h}$ is the measured noise in the H channel. The uniform sum is computed as

$$
\begin{equation*}
U S=\frac{1}{M} \sum_{i=0}^{M-1}\left|H_{i}\right|^{2}+\frac{1}{M} \sum_{i=0}^{M-1}\left|V_{i}\right|^{2}+\frac{1}{M-1}\left|\sum_{i=0}^{M-2} H_{i}^{*} H_{i+1}+\sum_{i=0}^{M-2} V_{i}^{*} V_{i+1}\right|+\frac{1}{M}\left|\sum_{i=0}^{M-1} H_{i}^{*} V_{i}\right| \tag{2}
\end{equation*}
$$

where * stands for the complex conjugate.
Let $T H R_{d B}$ be the SNR threshold specified in dB used in the legacy detector for the given variable (i.e., $Z$, $v$, or $\sigma_{v}$; for $Z_{D R}, \rho_{h v}$, and $\phi_{d p}$ the threshold is the same as for $Z$ ). The SNR threshold is computed as
$T H R_{S N R}=10^{\frac{T H R_{d B}}{10}}$.
The threshold for the "uniform sum" is computed as
$T H R_{U S}=\max \left(N_{h}, N_{v}\right) \cdot\left(\frac{\min \left(N_{h}, N_{v}\right)}{\max \left(N_{h}, N_{v}\right)}\right)^{B} \cdot \exp \left(A+C \cdot \frac{\min \left(N_{h}, N_{v}\right)}{\max \left(N_{h}, N_{v}\right)}\right)$,
where $N_{v}$ is the measured noise power in the vertical (V) channel, and the coefficients $A, B$, and $C$ are obtained from Table 1 . Note that each $M$ value has the corresponding set of coefficients associated to it. It is recommended that Table 1 be implemented so that the coefficients can be easily updated (e.g., as part of adaptation data or in a separate configuration file). Note that only a partial table is given in this paper, and a full table is provided in a separate file.

The step by step procedure of the proposed signal censoring algorithm that applies to each range gate is as follows.

```
if M > 89
    if SNRR
        accept as "significant return"
    else
        reject as "non-significant return"
    end
else
    if (SNR 
        accept as "significant return"
    else
        reject as "non-significant return"
    end
end
```

| $M$ | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $A$ | 1.4463 | 1.4367 | 1.4296 | 1.4044 | 1.3975 | 1.3615 | 1.3298 |
| $B$ | -0.1011 | $-8.9699 \mathrm{e}-2$ | -0.0863 | $-9.3613 \mathrm{e}-2$ | $-9.3940 \mathrm{e}-2$ | $-8.0318 \mathrm{e}-2$ | $-6.7912 \mathrm{e}-2$ |
| $C$ | 0.6126 | 0.59579 | 0.5898 | 0.59864 | 0.59725 | 0.58165 | 0.56929 |
| $M$ | 13 | 14 | 15 | 16 | 17 | 18 | 19 |
| $A$ | 1.3024 | 1.2576 | 1.239 | 1.1946 | 1.2039 | 1.1552 | 1.1511 |
| $B$ | $-5.5740 \mathrm{e}-2$ | $-6.1595 \mathrm{e}-2$ | $-4.8790 \mathrm{e}-2$ | $-3.9140 \mathrm{e}-2$ | $-2.9329 \mathrm{e}-2$ | $-4.5421 \mathrm{e}-2$ | $-2.9440 \mathrm{e}-2$ |
| $C$ | 0.55685 | 0.56567 | 0.55126 | 0.54377 | 0.52846 | 0.55309 | 0.53341 |
| $M$ | 20 | 21 | 22 | 23 | 24 | 25 | 26 |
| $A$ | 1.1223 | 1.1026 | 1.0953 | 1.0798 | 1.0691 | 1.0622 | 1.0454 |
| $B$ | $-3.2664 \mathrm{e}-2$ | $-3.1927 \mathrm{e}-2$ | $-2.1782 \mathrm{e}-2$ | $-1.8855 \mathrm{e}-2$ | $-1.3561 \mathrm{e}-2$ | $-6.1736 \mathrm{e}-3$ | $-6.1895 \mathrm{e}-3$ |
| $C$ | 0.54113 | 0.53956 | 0.52826 | 0.52593 | 0.51962 | 0.50996 | 0.51269 |
| $M$ | 27 | 28 | 29 | 30 | 31 | 32 | 33 |
| $A$ | 1.0313 | 1.028 | 1.0098 | 0.99348 | 0.99406 | 0.98481 | 0.98154 |
| $B$ | $-5.1542 \mathrm{e}-3$ | $2.1922 \mathrm{e}-3$ | $-2.6402 \mathrm{e}-4$ | $-2.9082 \mathrm{e}-3$ | $6.8651 \mathrm{e}-3$ | $9.0159 \mathrm{e}-3$ | $1.5671 \mathrm{e}-2$ |
| $C$ | 0.51222 | 0.50091 | 0.50718 | 0.51114 | 0.49914 | 0.49704 | 0.4895 |
| $M$ | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| $A$ | 0.96288 | 0.95693 | 0.94897 | 0.93505 | 0.93681 | 0.92138 | 0.9188 |
| $B$ | $9.7531 \mathrm{e}-3$ | $1.3140 \mathrm{e}-2$ | $1.5368 \mathrm{e}-2$ | $1.2681 \mathrm{e}-2$ | $2.0367 \mathrm{e}-2$ | $1.5745 \mathrm{e}-2$ | $2.0107 \mathrm{e}-2$ |
| $C$ | 0.49788 | 0.49382 | 0.49269 | 0.49756 | 0.48692 | 0.49384 | 0.48811 |
| $M$ | 41 | 42 | 43 | 44 | 45 | 46 | 47 |
| $A$ | 0.93523 | 0.90515 | 0.91548 | 0.89475 | 0.89016 | 0.89692 | 0.8842 |
| $B$ | $3.9809 \mathrm{e}-2$ | $2.2990 \mathrm{e}-2$ | $3.5888 \mathrm{e}-2$ | $2.6591 \mathrm{e}-2$ | $2.8431 \mathrm{e}-2$ | $3.9408 \mathrm{e}-2$ | $3.5303 \mathrm{e}-2$ |
| $C$ | 0.46344 | 0.48666 | 0.46772 | 0.48242 | 0.47995 | 0.46646 | 0.4728 |
| $M$ | 48 | 49 | 50 | 51 | 52 | 53 | 54 |
| $A$ | 0.87752 | 0.87178 | 0.86942 | 0.85894 | 0.85721 | 0.85255 | 0.83821 |
| $B$ | $3.5153 \mathrm{e}-2$ | $3.4939 \mathrm{e}-2$ | $3.8871 \mathrm{e}-2$ | $3.5241 \mathrm{e}-2$ | $3.9386 \mathrm{e}-2$ | $3.9818 \mathrm{e}-2$ | $3.3166 \mathrm{e}-2$ |
| $C$ | 0.47314 | 0.47245 | 0.46917 | 0.47388 | 0.47038 | 0.46945 | 0.47848 |

Table 1. Excerpt of the table with coefficients for the "uniform sum" threshold (THR ${ }_{U S}$ ) calculation as a function of the number of samples $M$. The complete table is provided in an electronic form as a separate file.

